

Emergent Acceleration from Quantum Gravity: Dynamical Dark Energy and Inflation

In collaboration with: T. Ladstätter and D. Oriti

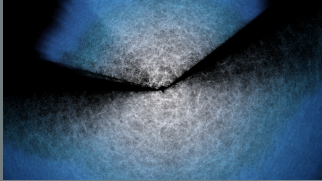
Luca Marchetti

13 Tux Winter Workshop on Quantum Gravity

Tux

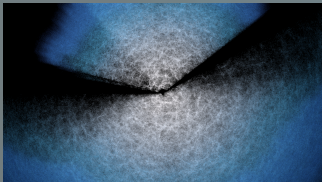
Feb 12, 2026

OIST
Kavli IPMU



The DESI galaxy survey

- ▶ BAOs create features in galaxy clusters of the size of the sound horizon at recombination.
- ▶ This is used as a ruler to determine the distance to different galaxies.
- ▶ In turn, this determines the Universe's evolution.

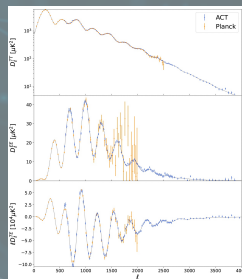


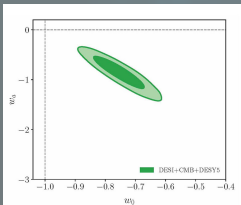
The ACT power spectra

- ▶ Ground based CMB observations.
- ▶ Higher angular resolution and targeted observation when compared to Planck.
- ▶ In practice: much smaller noise levels at small scales and extension to larger multipoles.

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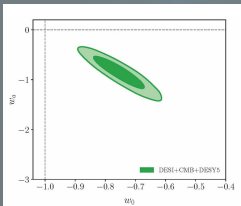
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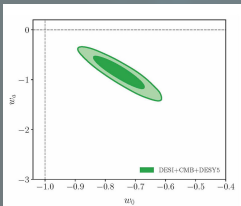
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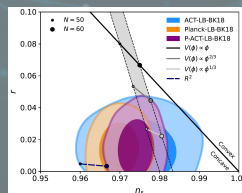
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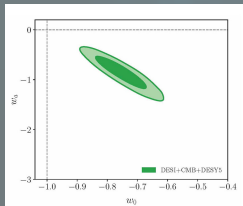
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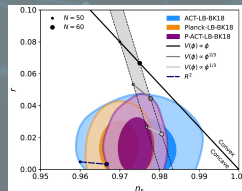
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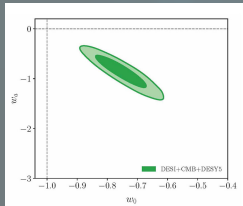
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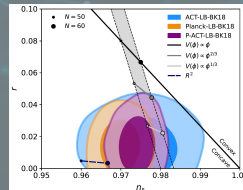
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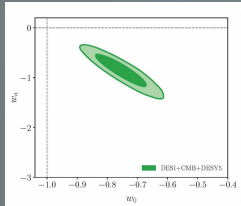
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Phantom dark energy models

- Fluid: violates NEC: which “matter”?
- Fundamental (k-essence): classical (gradient) & quantum instability (vacuum decay, ghosts).



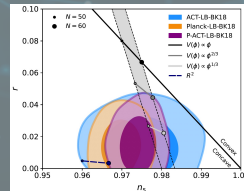


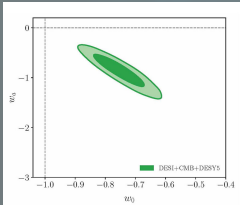
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- ▶ **Phenom.:** Increasingly large set of parameters with no clear physical interpretation.
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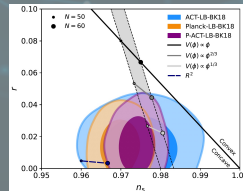


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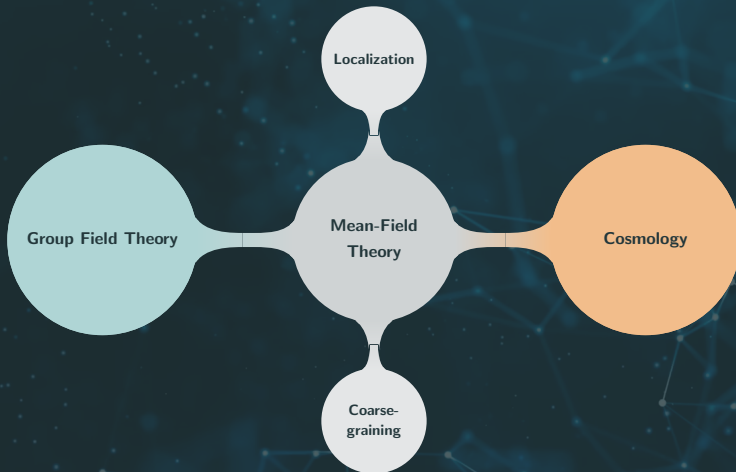
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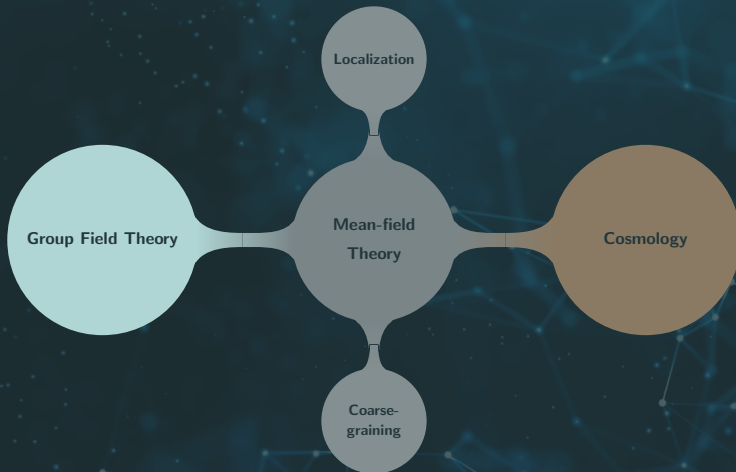
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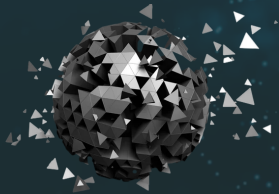
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Need for a paradigm shift?



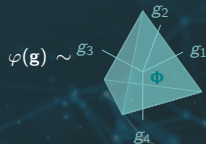


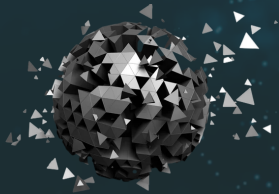


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Kinematics: GFT quanta

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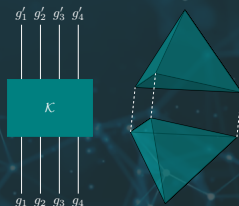


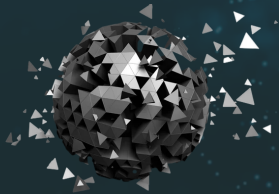


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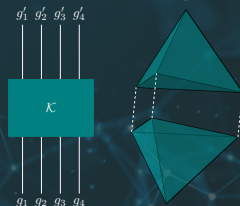


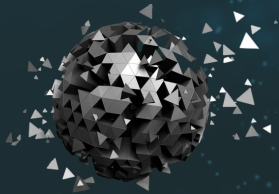


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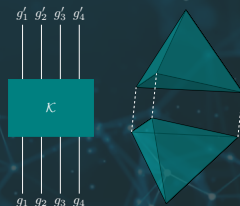




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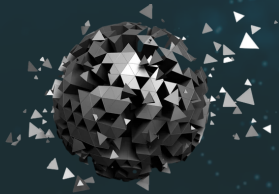
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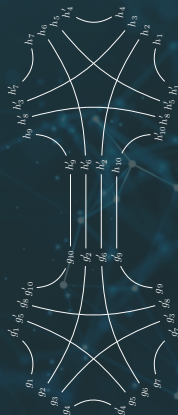
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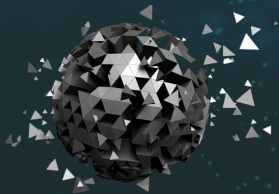
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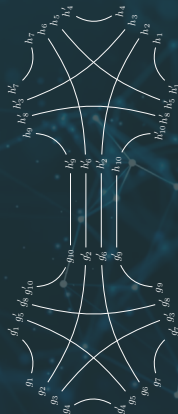
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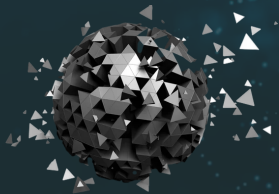
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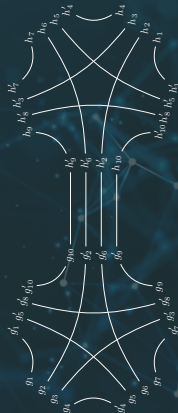
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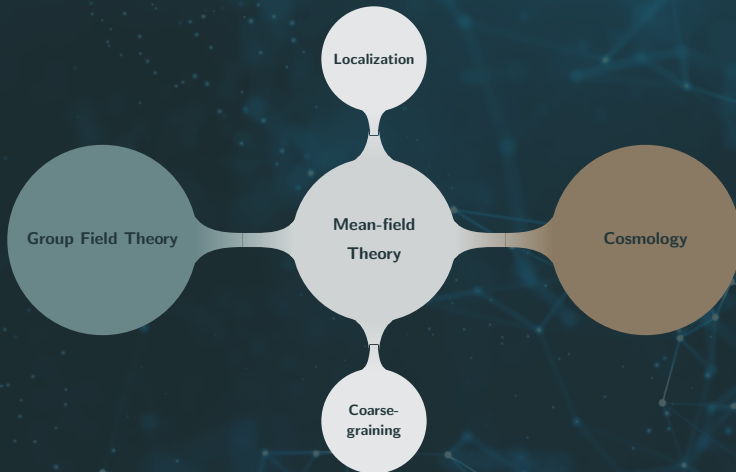
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- ▶ **Coarse-graining**

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Macroscopic Physics and Mean-Field Theory

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- ▶ Macroscopic physics captured by GFT mean-field σ (superspace density of GFT atoms) satisfying

$$\text{Relational effective dynamics: } \mathcal{K}[\sigma] + \mathcal{V}[\sigma, \sigma^*] = 0 .$$

Relational 2nd order differential operator ↑

↑ Non-local and non-linear.

- ▶ Can be obtained from $\langle \delta S_{\text{GFT}} / \delta \hat{\varphi}^\dagger \rangle_\sigma = 0$ where $|\sigma\rangle$ are frame-localized coherent states.

Effective methods

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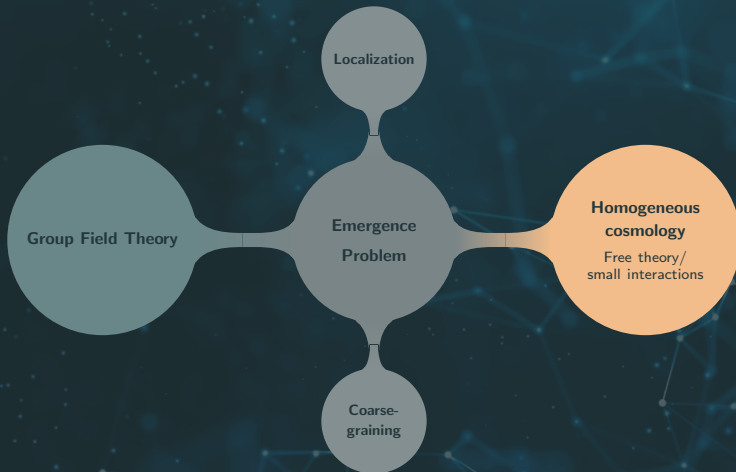
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Macroscopic quantities = Collective averages

$$\text{notation: } \varphi \cdot \psi = \int_{\mathcal{G}} \text{dg } \varphi \psi$$

- ▶ **Hydrodynamic**: Macroscopic quantities $\sim O_\sigma \sim \sigma$ -“hydrodynamic” averages of collective obs.
- ▶ Microscopic picture: Collective observables are one-body operators $\hat{\mathcal{O}}$ in $\mathcal{F}_{\text{GFT}}$: $\mathcal{O}_\sigma = \langle \hat{\mathcal{O}} \rangle_\sigma$.
- ▶ E.g. number $\hat{N} = \varphi^\dagger \cdot \hat{\varphi}$ and volume $\hat{V} = \hat{\varphi}^\dagger \cdot V[\hat{\varphi}]$, with $N_\sigma = \sigma^* \cdot \sigma$ and $V_\sigma = \sigma^* \cdot V[\sigma]$.

Effective methods



Effective FLRW cosmological dynamics

Mean-field approximation

- ▶ **Homogeneity:** σ depends on geometry + clock χ^0 .
- ▶ **Isotropy:** $\sigma_v \equiv \rho_v e^{i\theta_v}$ ($v_{\text{EPRL}} \in \mathbb{N}/2$, $v_{\text{BC}} \in \mathbb{R}$).
- ▶ **Mesoscopic regime:** negligible interactions.
- ▶ V_σ (thus a) increases as ρ_v (thus N_σ) increases.

$$0 = \mathcal{K}[\sigma],$$

$$\begin{aligned} V_\sigma(x^0) &= \sum_v V_v |\sigma_v|^2(x^0). \\ &= \bar{V}_0 a^3 \longrightarrow \{\mathcal{H}(V_\sigma), w(V_\sigma)\}. \end{aligned}$$

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Large/small number of quanta

- ✓ Volume quantum fluctuations under control.
- ✓ If one v_o is dominating and $\mu_{v_o}^2 = 3\pi G$, matching with relational GR dynamics:

$$(V'_\sigma/3V_\sigma)^2 \simeq 4\pi G/3 \longrightarrow \text{flat FLRW}$$

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$$\left(\frac{V'_\sigma}{3V_\sigma}\right)^2 = \left(\frac{2 \sum_v V_v \rho_v \text{sgn}(\rho'_v) \sqrt{\mathcal{E}_v - Q_v^2/\rho_v^2 + \mu_v^2 \rho_v^2}}{3 \sum_v V_v \rho_v^2}\right)^2, \quad \frac{V''_\sigma}{V_\sigma} = \frac{2 \sum_v V_v [\mathcal{E}_v + 2\mu_v^2 \rho_v^2]}{\sum_v V_v \rho_v^2}$$

Large/small number of quanta

- ✓ Volume quantum fluctuations under control.
- ✓ If one v_o is dominating and $\mu_{v_o}^2 = 3\pi G$, matching with relational GR dynamics:
- For a large range of initial conditions (at least one $Q_v \neq 0$ or one $\mathcal{E}_v < 0$)
- Same type of bouncing dynamics as in LQC.

$$(V'_\sigma/3V_\sigma)^2 \simeq 4\pi G/3 \longrightarrow \text{flat FLRW}$$

Singularity res. into quantum bounce!

Effective FLRW cosmological dynamics

Overview

Assumptions

- ▶ **Homogeneity:** $\sigma(g_A, \chi^0, \psi)$; ψ interacting scalar.
- ▶ **Isotropy:** $\sigma_v \equiv \rho_v e^{i\theta_v}$.
- ▶ **Weak interactions:** perturbative analysis.
- ▶ **Single spin:** only $v = v_o$ dominating.
- ▶ **Late times:** Large volumes (classical limit).

Dynamics

$$S[\phi, \phi^*] = \phi^* \cdot \mathcal{K}[\phi] + U[\phi, \phi^*]$$

$$\mathcal{K} = \mathcal{K}((\chi_1^0 - \chi_2^0)^2; (\psi_1 - \psi_2)^2)$$

$$U = U[\phi, \phi^*; V_\psi],$$

pseudo-simpl./tens. ↑

↑ ψ -potential

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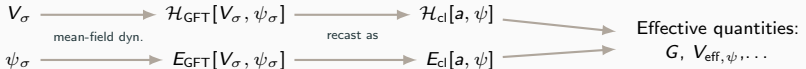
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Matching procedure



Models and Results

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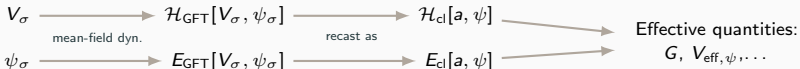
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Matching procedure



Pseudo-tensorial

$$U_{\text{T}}[\phi, \phi^*, V_\psi] = \text{Tr}\{\mathcal{U}_{\text{T}}[V_\psi] \phi^{\frac{l+1}{2}} (\phi^*)^{\frac{l+1}{2}}\}$$

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$$U_{\text{S}}[\phi, \phi^*, V_\psi] = \text{Tr}\{\mathcal{U}_{\text{S}}[V_\psi] \phi^{l+1}\} + \text{c.c.}$$

Models and Results

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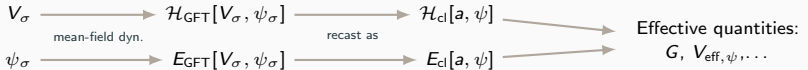
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- **Geometry:** matching + Λ for $l = 5$.

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Models and Results

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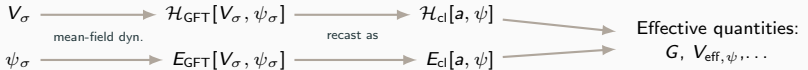
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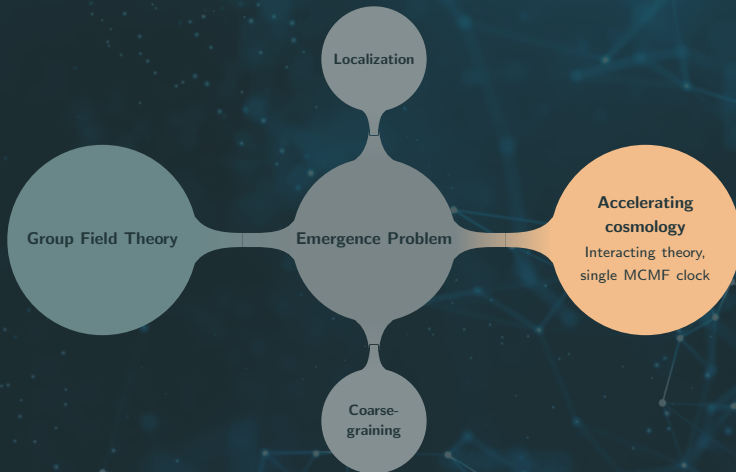
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- **Potential:** Matching only for a class of $\mathbf{V}_\psi$.

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- **QG-Higgs:** Emergence of (time-dep.) ψ -mass.
- **Potential:** Matching only for $V_{\text{eff}} \neq V_\psi$.

Models and Results



Emergent acceleration I: Stability

Model and Assumptions

$$\mathcal{K}_v[\sigma_v] + \mathcal{V}_v[\sigma_v, \sigma_v^*] = 0, \quad \mathcal{K}_v = \partial_\chi^2 - E_\chi^2, \quad \mathcal{V}_v[\sigma_v, \sigma_v^*] = -\lambda_v \rho_v e^{I \cdot i((m+1)\theta_v + \vartheta_v)},$$

Diagram annotations:

- kinetic kernel (points to $\mathcal{K}_v$)
- interaction kernel (points to $\mathcal{V}_v$)
- int. order $\in \mathbb{N}^+$ (points to I)
- $\in \mathbb{R}$ (points to λ_v)

- **Generalized mean-field:** Reduces to pseudo-tensorial/simplicial for $m = 0$ and $m = -(l + 1)$, resp.
- **Assumptions:** Homogeneity, isotropy, single-mode, late times. Interactions are non-perturbative.

Emergent acceleration I: Stability

Mean-field model

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Annotations: "kinetic kernel" points to $\mathcal{K}_v$; "interaction kernel" points to $\mathcal{V}_v$; "int. order $\in \mathbb{N}^+$ " points to the exponent; " $\in \mathbb{R}$ " points to λ_v .

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Dynamical system

Fixed points and dynamical stability

- First order for $x = \theta$, $y = \rho' / \rho^3$, $z = \theta'$.
- **FP_∞:** $l=5$, $\bar{y}^2 = |\lambda|/3$, $\bar{x} = (n\pi - \vartheta)/m$, $z=0$.
- FP_∞ dynam. (weak) attractor iff $1+3m/4 < 0$.

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Cosmological stability: y -behavior

$$H^2 \propto y^2, \quad w = -[(1 + y'/(y^2))]$$

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Emergent acceleration I: Stability

Mean-field model

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Dynamical system

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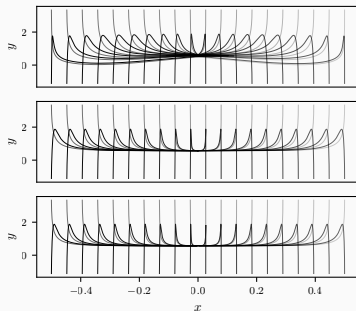
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Emergent dS **cosmological attractor** for $m \leq 0$.



Emergent acceleration I: Stability

Mean-field model

Model and Assumptions

$$\begin{aligned} \text{kinetic kernel} \quad \mathcal{K}_v[\sigma_v] + \text{interaction kernel} \quad \mathcal{V}_v[\sigma_v, \sigma_v^*] &= 0, & \mathcal{K}_v &= \partial_x^2 - E_x^2, & \mathcal{V}_v[\sigma_v, \sigma_v^*] &= -\lambda_v \rho_v e^{l i((m+1)\theta_v + \vartheta_v)}, \\ & & & & \text{int. order } \in \mathbb{N}^+ & \\ & & & & \in \mathbb{R} & \end{aligned}$$

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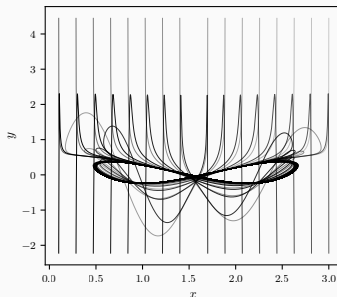
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Emergent dS **cosmologically unstable** for $m > 0$.



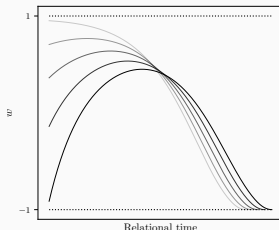
Emergent acceleration II: Dynamical Dark Energy

Asymptotic Λ

- Emergent DE: For $m \leq 0$ asymptotic dS attractor.

$$\bar{w} = -1, \quad \bar{\Lambda} = |\lambda| \frac{4\pi^2}{9v^2}$$

GFT coupling $\downarrow$ Clock momentum $\downarrow$
Volume eigenvalue $\uparrow$



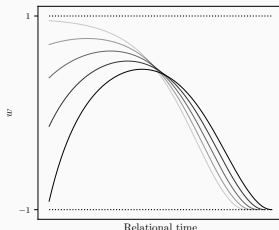
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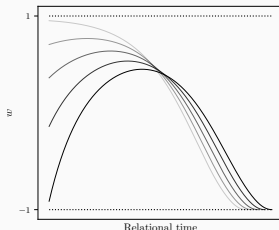
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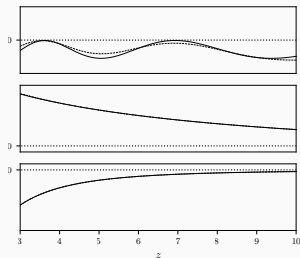


Dynamical behavior

EoS dynamics

$$\delta w(z) = \begin{cases} \overbrace{[\mathcal{T}(z)]^{-6}(\delta w_0 + \delta w_1 \cos 2\Phi(z) + \delta w_2 \sin 2\Phi(z))}^{\downarrow (1+z_q)/(1+z)} & \overbrace{\propto \mathcal{T}(z)}^{\downarrow \propto \mathcal{T}(z)} \\ \delta w_0 [\mathcal{T}(z)]^{6(\sqrt{1+3m/4}-1)} & \text{Solutions depend} \\ \delta w_0 [\mathcal{T}(z)]^{-6} \log^2[\mathcal{T}(z)] & \text{on } \text{sgn}(1+3m/4). \end{cases}$$

- **Quantum features:** $z_q \sim \#$ of QG atoms today.



Emergent acceleration II: Dynamical Dark Energy

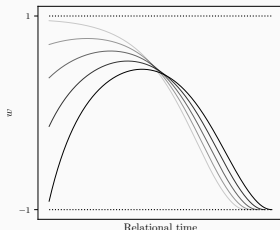
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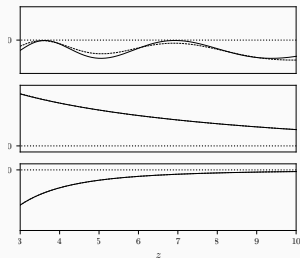


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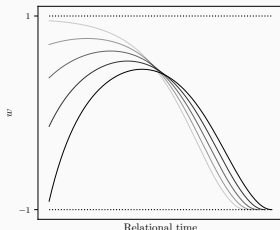
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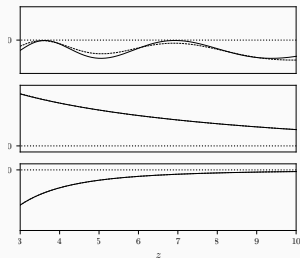
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Emergent dynamical (typically phantom) dark energy!



Emergent acceleration III: Emergent Inflation

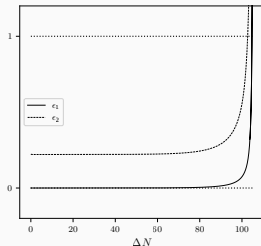
Slow-Roll Inflation

- **Quasi dS:** For $m > 0$ FP_∞ repulsive; acceleration ends.

$$\epsilon_1(N) = \exp[-\epsilon_2(N_{\text{end}} - N)]$$

$$\epsilon_2(N) = 6(\mu - 1)$$

$$\uparrow (1 + 3m/4)^{1/2}$$



Emergent acceleration III: Emergent Inflation

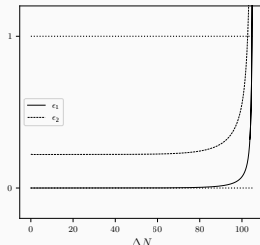
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- ▶ **Graceful exit:** Inflation ends after $N_{\text{end}} \gg 1$.



Emergent acceleration III: Emergent Inflation

Quasi dS phase

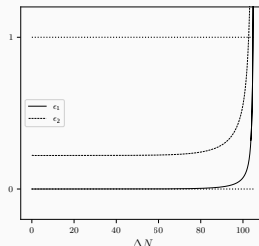
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Single-field description

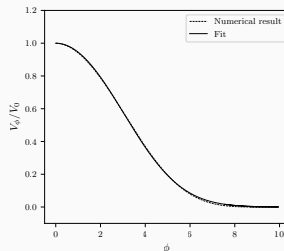
Emergent Inflaton

- ▶ **SFI:** GFT inflation can be described by emergent ϕ :

$$\delta\theta(\phi) \propto \phi - \phi_0$$

$$V(\phi) = V_0 \left(1 - \frac{(\phi - \phi_0)^2}{3} \right) e^{-2(\phi - \phi_0)^2 / \epsilon_2}, \quad \phi \in [\phi_0, \phi_0 + 1]$$

Annotations: A light blue arrow points from "GFT phase" to the $(\phi - \phi_0)^2$ term. Another light blue arrow points from the domain $\phi \in [\phi_0, \phi_0 + 1]$ to the exponential term.



Emergent acceleration III: Emergent Inflation

Quasi dS phase

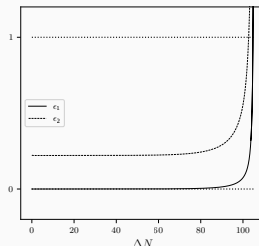
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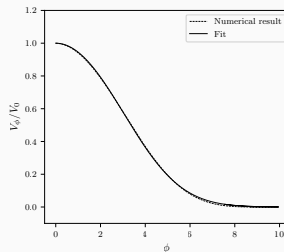
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$$V(\phi) = V_0 \left(1 - \frac{(\phi - \phi_0)^2}{3} \right) e^{-2(\phi - \phi_0)^2 / \epsilon_2},$$

Emergent slow-roll single-field inflation!



Dynamical Dark Energy

- ▶ Order 6 GFT interactions **generate acceleration**, both in pseudo-tensorial/-simplicial models.
- ▶ For $m \leq 0$ **de Sitter is an asymptotic attractor**, with Λ depending on GFT parameters.
- ▶ Emergent **dynamical dark energy**, with $w = w(z)$ depending on the microscopic parameters.
- ▶ Dark energy is **phantom** for a large set of models (including pseudo-simplicial)!

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- ▶ Slow-roll: for $m \ll 1$ emergent inflation is slow-roll, so large e-folds without fine tuning.
- ▶ Emergent inflaton: dynamics can be described as SFI; inflaton associated with condensate phase.
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Model Building and Phenomenology

- ⚠ How do predictions on $w(z)$ compare with data?
- ▶ How do primordial cosmological perturbations emerge from QG? (No inflaton in this model)
- ⚠ In this scenario, what can cosmological power spectra tell us about QG?
- ⚠ Can a similar mechanism also produce a dark matter component? (No dark matter in this model)
- ▶ Constraining effective theory space: map between SFI models and GFT mean-field theory models?
- ▶ Impact of additional modes on emergent dynamical dark energy behavior?
- ▶ ...